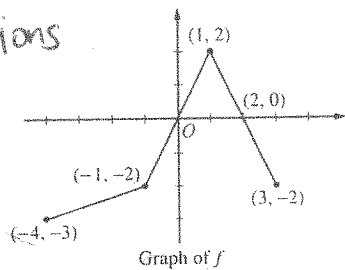


# AP Calculus Review + Applications

## FRA STRAWBERRY SET

2005B NO CALC

4. The graph of the function  $f$  above consists of three line segments.



- Let  $g$  be the function given by  $g(x) = \int_{-4}^x f(t) dt$ . For each of  $g(-1)$ ,  $g'(-1)$ , and  $g''(-1)$ , find the value or state that it does not exist.
- For the function  $g$  defined in part (a), find the  $x$ -coordinate of each point of inflection of the graph of  $g$  on the open interval  $-4 < x < 3$ . Explain your reasoning.
- Let  $h$  be the function given by  $h(x) = \int_x^3 f(t) dt$ . Find all values of  $x$  in the closed interval  $-4 \leq x \leq 3$  for which  $h(x) = 0$ .
- For the function  $h$  defined in part (c), find all intervals on which  $h$  is decreasing. Explain your reasoning.

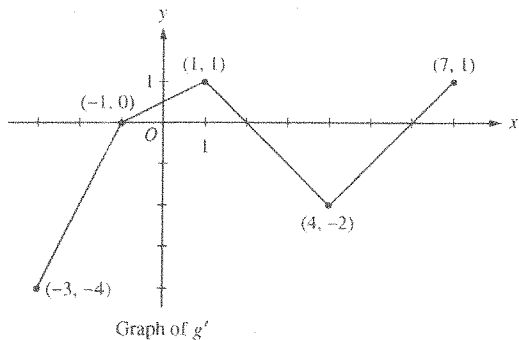
2008B NO CALC

4. The functions  $f$  and  $g$  are given by  $f(x) = \int_0^{3x} \sqrt{4+t^2} dt$  and  $g(x) = f(\sin x)$ .

- Find  $f'(x)$  and  $g'(x)$ .
- Write an equation for the line tangent to the graph of  $y = g(x)$  at  $x = \pi$ .
- Write, but do not evaluate, an integral expression that represents the maximum value of  $g$  on the interval  $0 \leq x \leq \pi$ . Justify your answer.

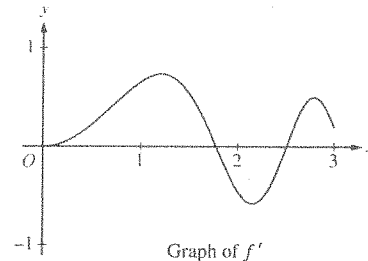
2008B

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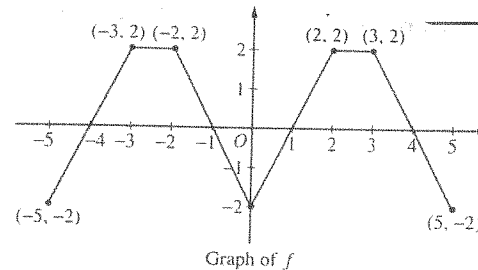
5. Let  $g$  be a continuous function with  $g(2) = 5$ . The graph of the piecewise-linear function  $g'$ , the derivative of  $g$ , is shown above for  $-3 \leq x \leq 7$ .
- Find the  $x$ -coordinate of all points of inflection of the graph of  $y = g(x)$  for  $-3 < x < 7$ . Justify your answer.
  - Find the absolute maximum value of  $g$  on the interval  $-3 \leq x \leq 7$ . Justify your answer.
  - Find the average rate of change of  $g(x)$  on the interval  $-3 \leq x \leq 7$ .
  - Find the average rate of change of  $g'(x)$  on the interval  $-3 \leq x \leq 7$ . Does the Mean Value Theorem applied on the interval  $-3 \leq x \leq 7$  guarantee a value of  $c$ , for  $-3 < c < 7$ , such that  $g''(c)$  is equal to this average rate of change? Why or why not?

2006B  
YES  
CALC.



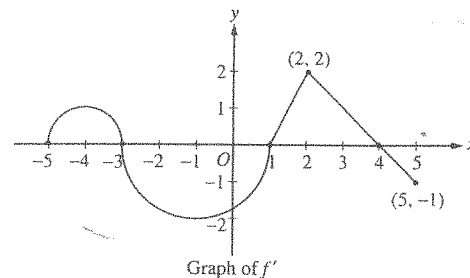
2. Let  $f$  be the function defined for  $x \geq 0$  with  $f(0) = 5$  and  $f'$ , the first derivative of  $f$ , given by  $f'(x) = e^{(-x/4)} \sin(x^2)$ . The graph of  $y = f'(x)$  is shown above.
- Use the graph of  $f'$  to determine whether the graph of  $f$  is concave up, concave down, or neither on the interval  $1.7 < x < 1.9$ . Explain your reasoning.
  - On the interval  $0 \leq x \leq 3$ , find the value of  $x$  at which  $f$  has an absolute maximum. Justify your answer.
  - Write an equation for the line tangent to the graph of  $f$  at  $x = 2$ .

2006A  
YES  
CALC



3. The graph of the function  $f$  shown above consists of six line segments. Let  $g$  be the function given by  $g(x) = \int_0^x f(t) dt$ .
- Find  $g(4)$ ,  $g'(4)$ , and  $g''(4)$ .
  - Does  $g$  have a relative minimum, a relative maximum, or neither at  $x = 1$ ? Justify your answer.
  - Suppose that  $f$  is defined for all real numbers  $x$  and is periodic with a period of length 5. The graph above shows two periods of  $f$ . Given that  $g(5) = 2$ , find  $g(10)$  and write an equation for the line tangent to the graph of  $g$  at  $x = 108$ .

2007B  
NO CALCULATOR



4. Let  $f$  be a function defined on the closed interval  $-5 \leq x \leq 5$  with  $f(1) = 3$ . The graph of  $f'$ , the derivative of  $f$ , consists of two semicircles and two line segments, as shown above.
- For  $-5 < x < 5$ , find all values  $x$  at which  $f$  has a relative maximum. Justify your answer.
  - For  $-5 < x < 5$ , find all values  $x$  at which the graph of  $f$  has a point of inflection. Justify your answer.
  - Find all intervals on which the graph of  $f$  is concave up and also has positive slope. Explain your reasoning.
  - Find the absolute minimum value of  $f(x)$  over the closed interval  $-5 \leq x \leq 5$ . Explain your reasoning.