

Logarithms

DATE _____ Per. _____

6. The competition between the two banks is escalating and creating tedious work for everyone. They started compounding interest rates every hour, and then every minute, and finally, every second. Several factors complicated the process. The employees started to complain about carpal tunnel syndrome in their fingers from pressing all the calculator buttons. Many calculators broke and had to be replaced. Then interest rates changed and all the numbers previously worked out were no longer valid. Someone thought there must be a better way. So **Lenders' National** hired a mathematician to develop an equation that gives the principal balance P using the following variables:

| |
|--|
| $d =$ initial deposit $r =$ interest rate percent $n =$ # of times compounded per year |
|--|

a) What is this equation?

 $P =$

7. Use this new equation to determine the balance for an account with:

- a) \$5,000 deposit on 8% compounded hourly =
- b) \$10,000 deposit on 5.5% compounded every minute =
- c) \$50,000 deposit on 3.25% compounded every second =

8. Now the banks want to know if there is a limit if they compound 100% interest rate continuously (that is infinitely many times per year). The **Bank of e** wants you to find the limit "e" by filling in the table.

| | A | B | C |
|----|---------------|----------|---------------|
| 1 | COMPOUNDED | n | $(1 + 1/n)^n$ |
| 2 | annually | 1 | 2 |
| 3 | semi-annually | 2 | |
| 4 | 3 times/year | | 2.3703703704 |
| 5 | quarterly | | |
| 6 | bi-monthly | 6 | |
| 7 | | 12 | 2.6130352902 |
| 8 | | 52 | |
| 9 | daily | | |
| 10 | hourly | | |
| 11 | every minute | 525600 | 2.7182792426 |
| 12 | every second | 31536000 | |

9. a) What value is e ?

b) How is this number like π ?

10. Punch these buttons in your calculator to find \$1,000 compounded continuously at 12%.

a) $1000 \times e^{0.12} =$

b) How does this amount compare with all other methods of compounding?