

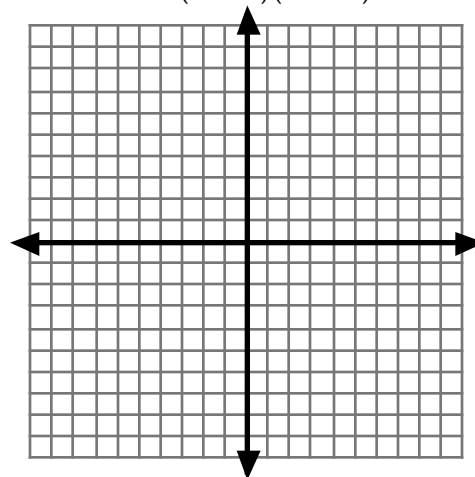
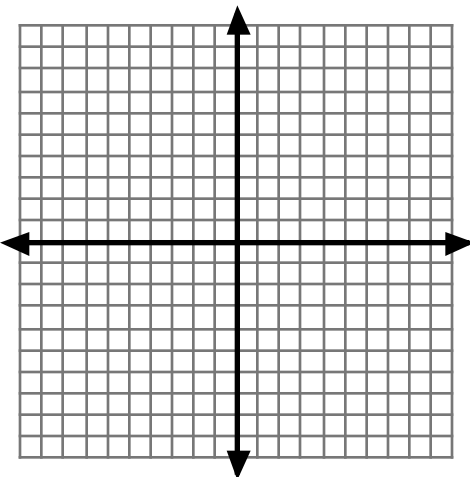
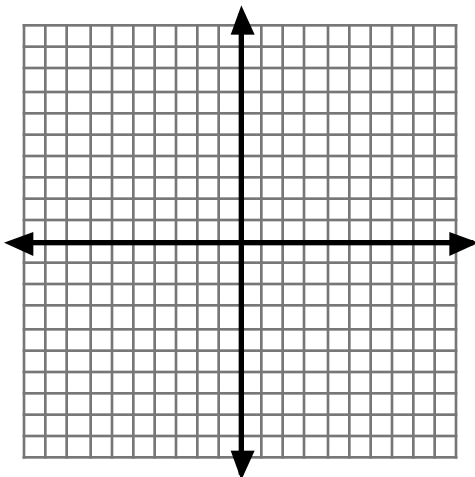
(Press ZOOM - 6 to standardize your window, and then ZOOM - 5 to square it.)

1. Graph the following equations by pressing Y= and entering each expression. Then draw graph.

a)  $y = (x - 3)(x + 1)$

b)  $y = x(x - 2)(x + 3)$

c)  $y = (x^2 - 1)(x^2 - 4)$



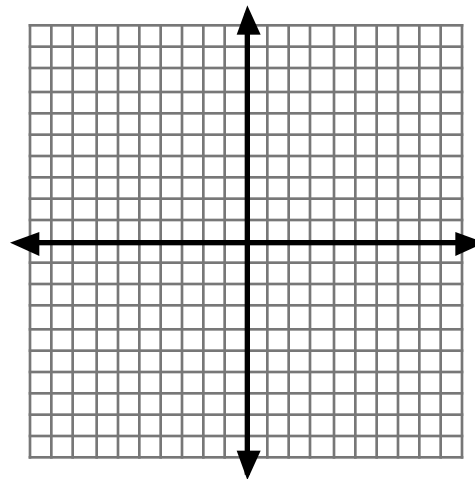
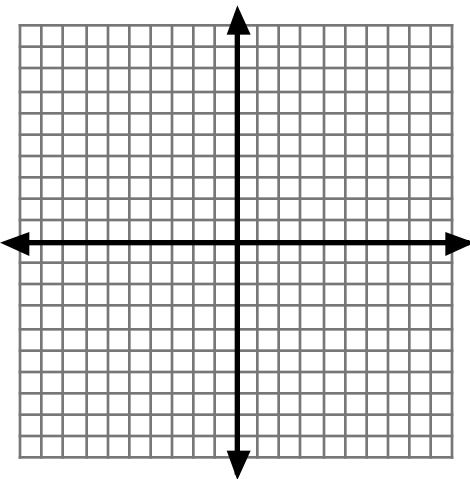
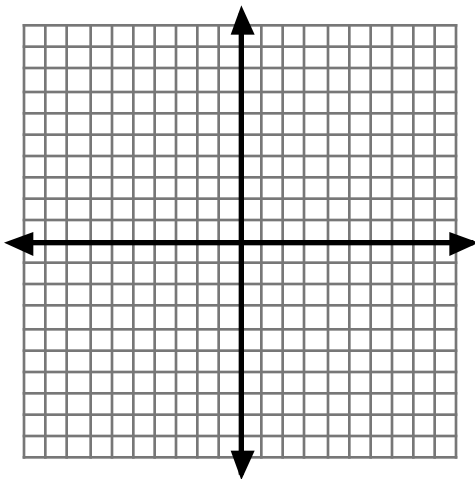
- d) How many times does the quadratic polynomial cross the  $x$ -axis?      The cubic?      Quartic?  
 e) What are the  $x$ -intercepts in part a?      Part b's graph?      Part c?  
 f) Which graph has symmetry over the  $y$ -axis (i.e. an even function with  $p(x) = p(-x)$ )?

2. Graph the following equations. :

a)  $y = (x - 3)(x + 1)^2$

b)  $y = (x - 1)^2(x + 1)^2$

c)  $y = x(x - 2)^2(x + 2)^2$



- d) Where does each graph "bounce" off the  $x$ -axis?  
 e) How could you tell where it bounces from looking at the equation without graphing?  
 f) Each "bounce" matches a repeated factor with an exponent  $> 1$ . e.g.  $(x - 3)^2$  has a multiplicity of 2 at  $x = 3$ .  
 Write an equation that has a multiplicity of 2 at  $x = 1$ .

3. a) Write an equation of a polynomial that crosses the  $x$ -axis at  $(0, 0)$ ,  $(0, 1)$ ,  $(0, -1)$ ,  $(0, 2)$  and  $(0, -3)$

b) Identify the multiplicities and  $x$ -intercepts of  $y = (x - 0)(x - 1)^2(x + 4)^3$ .

c) Finish factoring to find all  $x$ -intercepts of  $y = (x^2 - 1)(x^2 - 9)(x^2 - x - 6)$ .  
 Are there any multiplicities?